

Natural Circulation Salt Heat Transfer

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Session 7: Support for Salt Technologies



Prandtl Number of Different Fluids

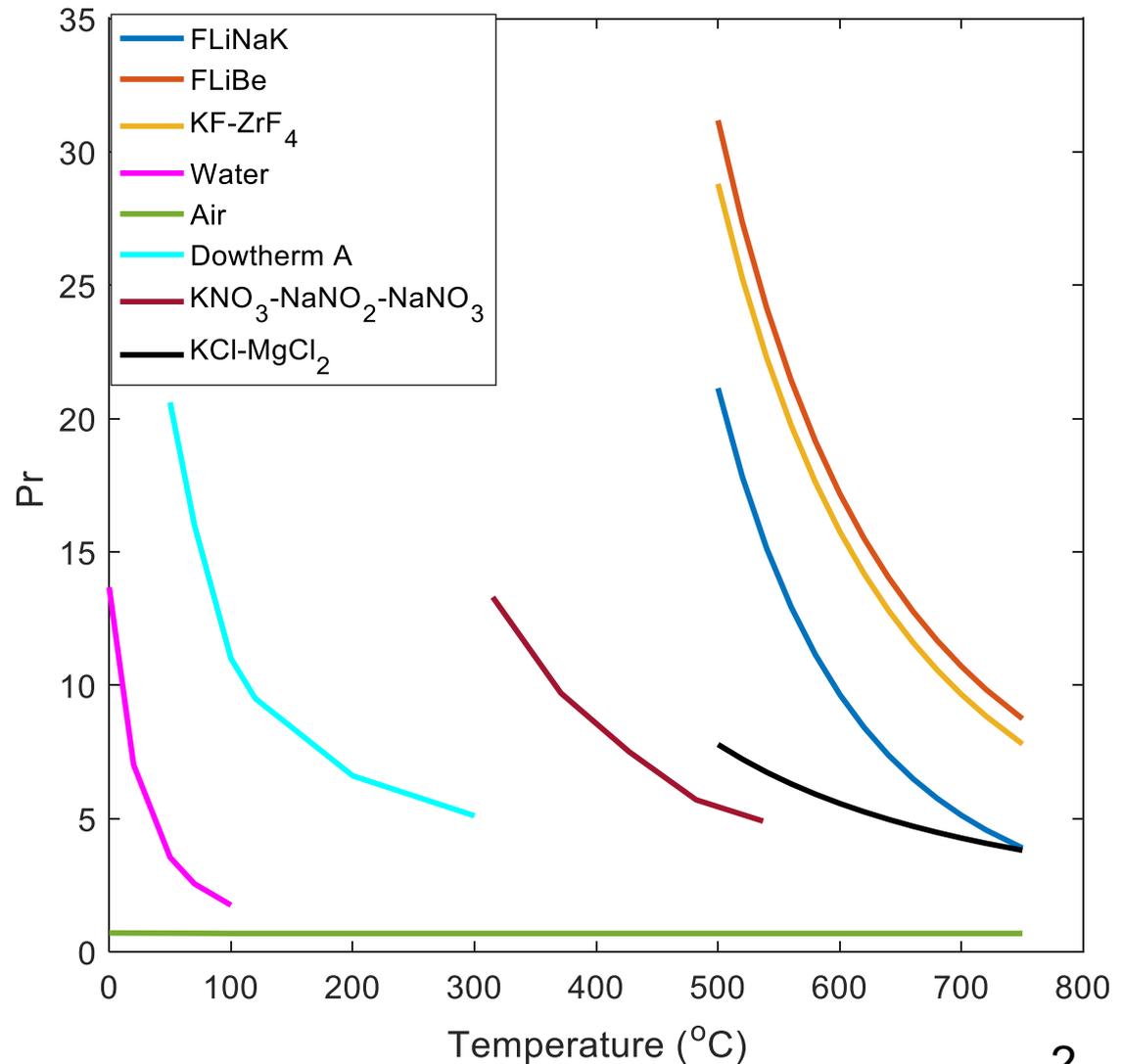
- Liquid Salts

- FLiBe
- FLiNaK
- KF-ZrF₄
- KCl-MgCl₂
- KNO₃-NaNO₂-NaNO₃

- Water

- Dowtherm A

- Air



Natural/Forced Convection Heat Transfer Coefficient Correlations

Natural Convection (NC)/Forced Convection (FC)	Correlation	Geometry	Working fluid	Pr range	Ra or Re range	Ref.
NC	$\sqrt{Nu} = 0.825 + \frac{0.387Ra^{1/6}}{\left[1 + \left(\frac{0.437}{Pr}\right)^{9/16}\right]^{8/27}}$	Vertical plate	Sodium, mercury, air, water, oil	$0.004 \leq Pr \leq 300$	$Ra \leq 10^{12}$	[1]
NC	$Nu = 0.54Ra^{1/4}$	Horizontal plate, hot surface facing up	Air	$Pr = 0.7$	$10^5 \leq Ra \leq 2 \times 10^7$	[2]
NC	$Nu = 0.27Ra^{1/4}$	Horizontal plate, hot surface facing down	Air	$Pr = 0.7$	$3 \times 10^5 \leq Ra \leq 10^{10}$	[2]
NC	$Nu = 0.474Ra^{0.25}Pr^{0.047}$	Horizontal cylinder	Air, water, silicone oils	$0.7 \leq Pr \leq 3090$	$3 \times 10^2 \leq Ra \leq 2 \times 10^7$	[3]

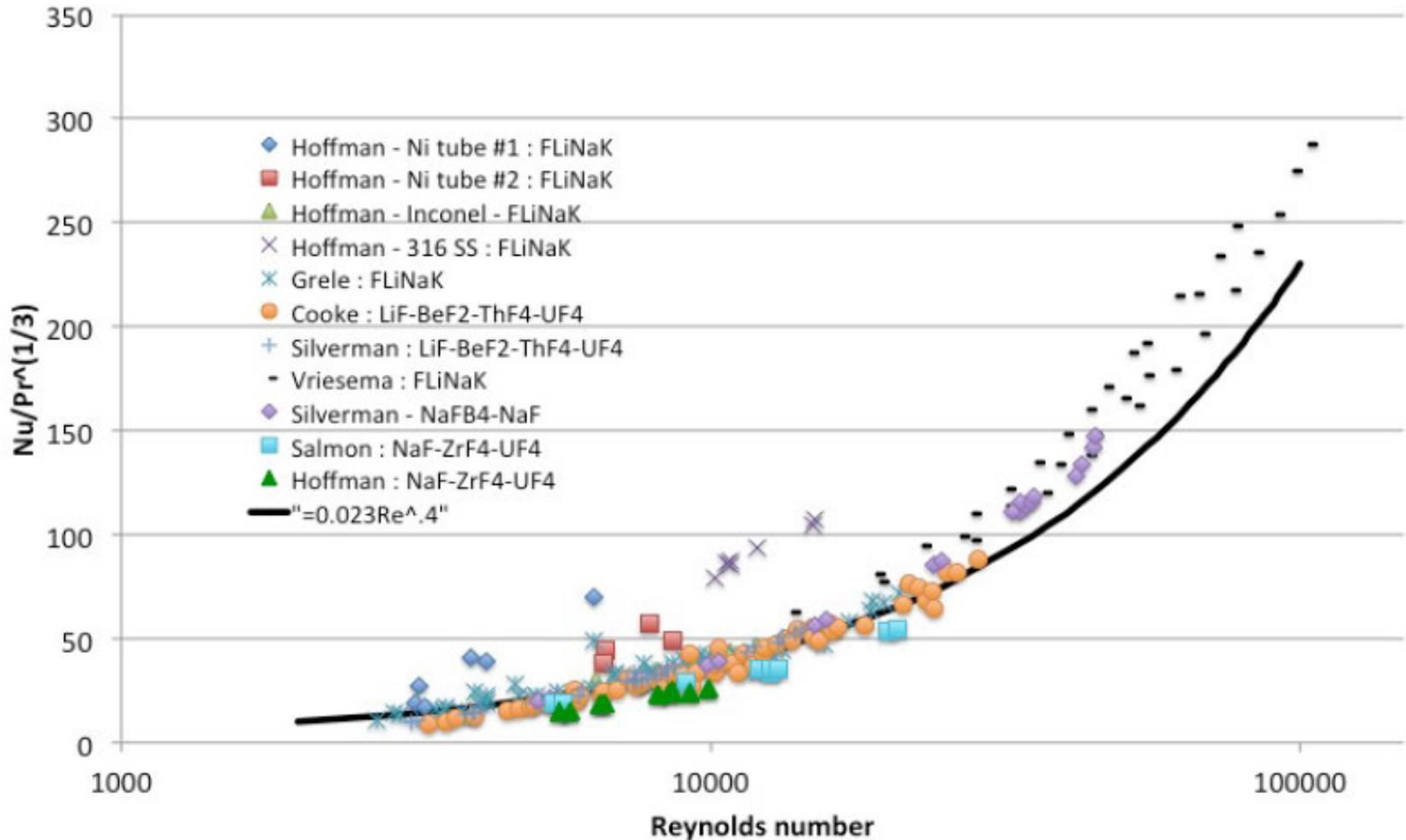
Natural/Forced Convection HTC Correlations (Cont'd)

Natural Convection (NC)/Forced Convection (FC)	Correlation	Geometry	Working fluid	Pr range	Ra or Re range	Ref.
NC	$\text{Nu} = 2 + \frac{0.589\text{Ra}^{1/4}}{\left[1 + \left(\frac{0.469}{\text{Pr}}\right)^{9/16}\right]^{4/9}}$	Spheres	air, water, oil	$\text{Pr} \geq 0.7$	$\text{Ra} \leq 10^{11}$	[4]
FC	$\text{Nu} = 0.027\text{Re}^{0.8}\text{Pr}^{1/3}(\mu/\mu_s)^{0.14}$	Pipe	air, water, oil	$0.7 \leq \text{Pr} \leq 16700$	$\text{Re} \geq 10^4$	[5]
FC	$\text{Nu} = 1.86\text{Re}^{1/3}\text{Pr}^{1/3} \left(\frac{D}{L}\right)^{1/3} (\mu/\mu_s)^{0.14}$	Pipe	air, water, oil	$0.7 \leq \text{Pr} \leq 16700$	$\text{Re} \leq 2300$	[6]
FC	$\text{Nu} = 0.116(\text{Re}^{2/3} - 125)\text{Pr}^{1/3}(\mu/\mu_s)^{0.14}$	Pipe	air, water, oil	$0.7 \leq \text{Pr} \leq 3$	$3500 \leq \text{Re} \leq 1.2 \times 10^4$	[7]

Natural/Forced Convection HTC Correlations (Cont'd)

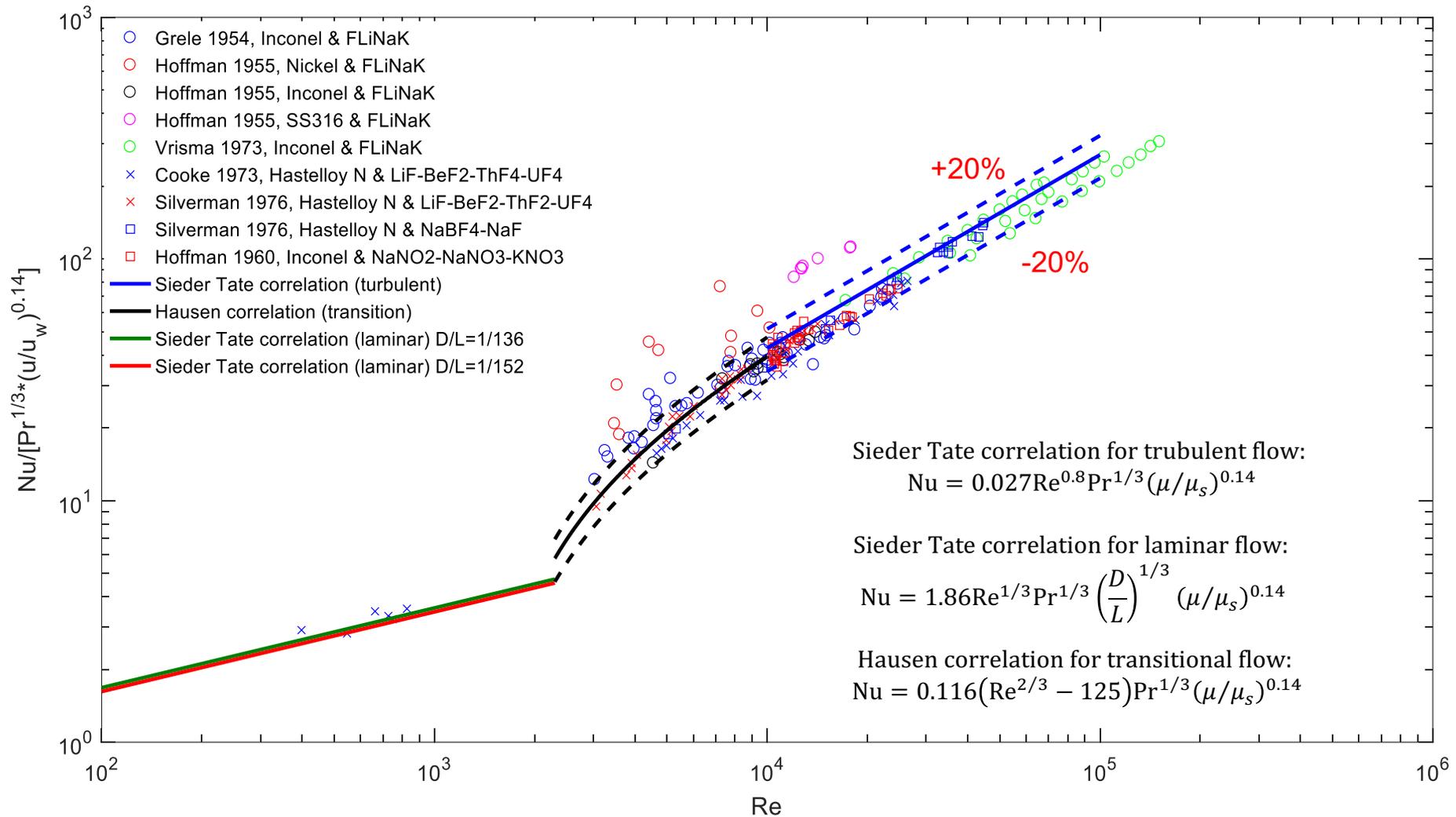
Natural Convection (NC)/Forced Convection (FC)	Correlation	Geometry	Working fluid	Pr range	Ra or Re range	Ref.
FC	$\text{Nu} = 0.023\text{Re}^{0.8}\text{Pr}^n$ $n = 0.4 \text{ if the fluid is heated}$ $n = 0.3 \text{ if the fluid is cooled}$	Pipe	air, water, oil	$0.7 \leq \text{Pr} \leq 100$	$\text{Re} \geq 10^4$	[8]
FC	$\text{Nu} = 2 + \left(0.4\text{Re}^{0.5} + 0.06\text{Re}^{2/3}\right)\text{Pr}^{0.4}$	Sphere	air, water, oil	$0.7 \leq \text{Pr} \leq 380$	$\text{Re} \leq 7.6 \times 10^4$	[9]
FC	$\text{Nu} = 0.023\text{Re}^{0.8}\text{Pr}^{1/3}$	Pipe	air, water, oil	$0.7 \leq \text{Pr} \leq 100$	$\text{Re} \geq 10^4$	[10]

Comparison of Colburn Correlation with Salt Forced Circulation Experiments



(G. Yoder, 2014)

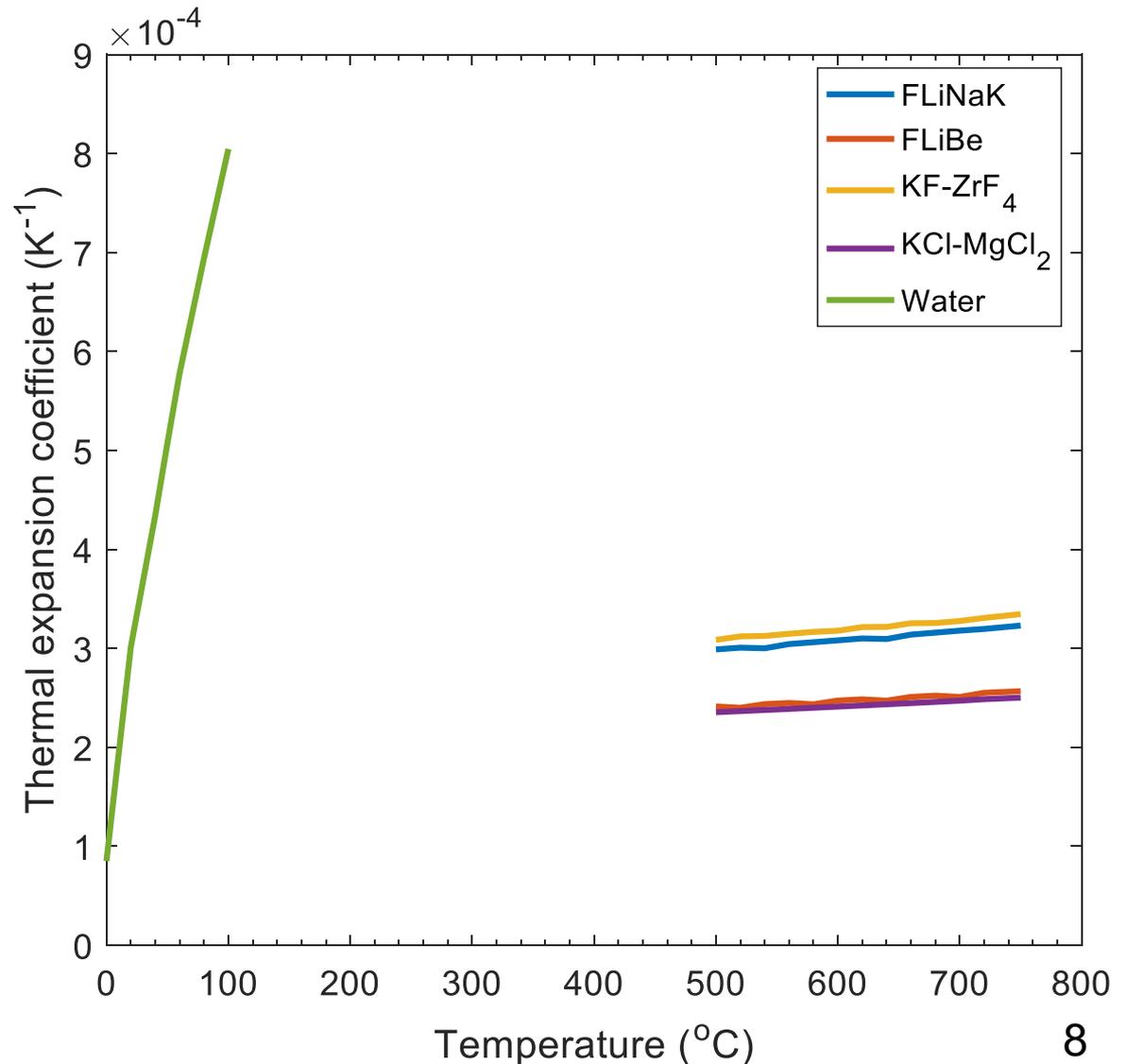
Comparison with Salt Forced Circulation Experiments



Thermal Expansion Coefficient for Different Fluids

- FLiBe
- FLiNaK
- KF-ZrF₄
- KCl-MgCl₂
- H₂O (1 atm)

$$\Delta p = (\rho_0 \beta \Delta T) g \Delta h$$



Review of Natural/Forced Circulation Loops for MSR/FHRs

Organization	NC/FC	Experiment Modeling	Objective	Material	Working fluid	Max working temp. (°C)	at max temp. (K ⁻¹)	Max power (kW)	Ref.
Oak Ridge National Laboratory, USA	NC	Experiment	Preparation for operation of the MSRE	Hastelloy N Single loop	LiF-BeF ₂ -ZrF ₄ -UF ₄	784	--	30,000	[11]
					LiF-BeF ₂ -ZrF ₄	670		8.8	
	NC	Experiment Fluent	a) Determine if the experimental configuration provides sufficient salt velocity for collection of corrosion data; b) Quantify natural circulation salt velocities using a laser Doppler velocimeter;	Nickel crucible	FLiNaK	700	0.00032	0.5	[12] [13]
FC	Experiment	a) Develop a nonintrusive, inductive heating technique b) Measure heat transfer characteristics	Inconel 600 single loop		200				
The Ohio State University (University of Michigan), USA	NC	Experiment Relap5 MOD 4.0	Examine the couplings among the natural circulation/convection loops and provide experience for high-temperature DRACS loop design	SS 304 coupled loops	Water	76.5	0.00061	2	[14] [15]
	NC	Experiment	Investigate DRACS performance under steady-state and transient conditions, including startup, pump trip test w/o IHX	SS 316 coupled loops	FLiNaK	722	0.00032	70	

Review of Natural/Forced Circulation Loops for MSR/FHRs (Cont'd)

Organization	FC/NC	Experiment Modeling	Objective	Material	Working fluid	Max working temp. (°C)	at max temp. (K ⁻¹)	Max power (kW)	Ref.
University of California, Berkeley, USA	NC/FC	Experiment Relap5-3D modeling	Provide experimental validation data for system-level thermal hydraulic codes; Serve as an advanced reactor test bed;	Stainless steel/copper	Dowtherm A	120	0.00075	10	[16] [17]
University of New Mexico, USA	NC/FC	Experiment	System code validation; Heat exchanger testing	Stainless steel single loop	Dowtherm A	--	--	20	[18]
University of Wisconsin, USA	NC	Experiment Fluent	Research in natural circulation stability, salt freezing, etc.	--	FLiBe	800	0.00027	--	[19]
	FC	Experiment	Identify salt corrosion and heat transfer issues	SS 316 Single loop	KCl-MgCl ₂	600	0.00029	4	[20]
US Industry	NC/FC	Experiment	Gaining operation experience with salts, corrosion, component testing, instrumentation, etc.		Salts				
Ulsan National Institute of Science and Technology, Korea	NC	Experiment MARS code modeling	Understand the thermal-hydraulic characteristics of molten salts using simulants	SS 304 Single loop	Dowtherm RP	80	0.00071	0.3	[21]

Review of Natural/Forced Circulation Loops for MSR/FHR (Cont'd)

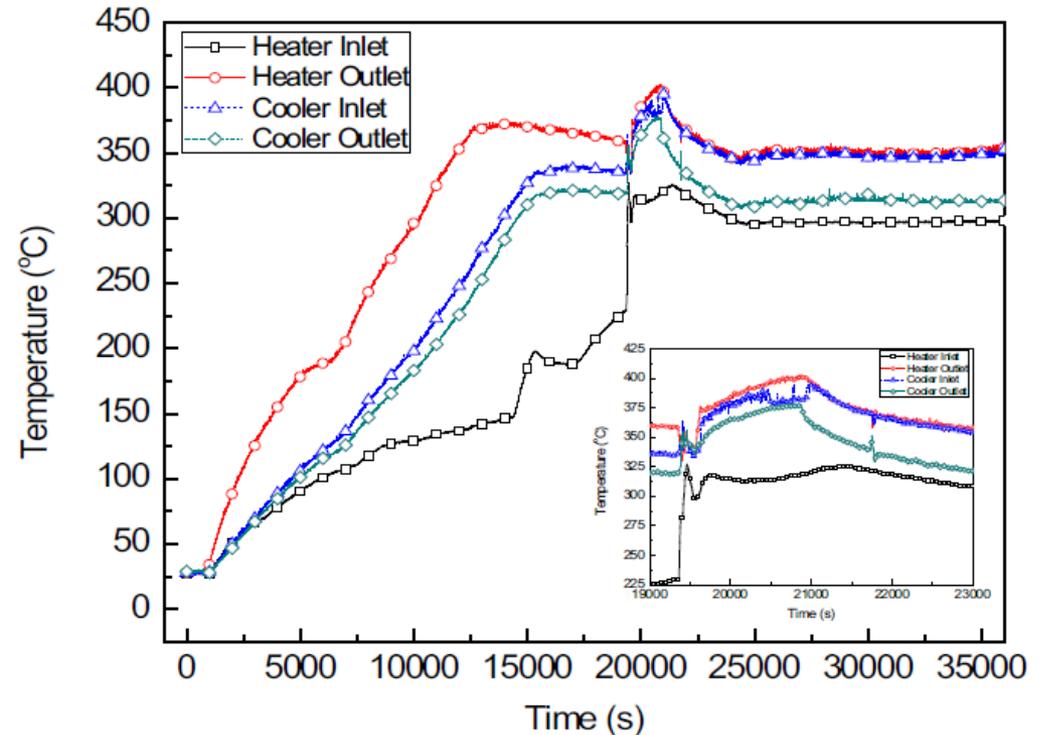
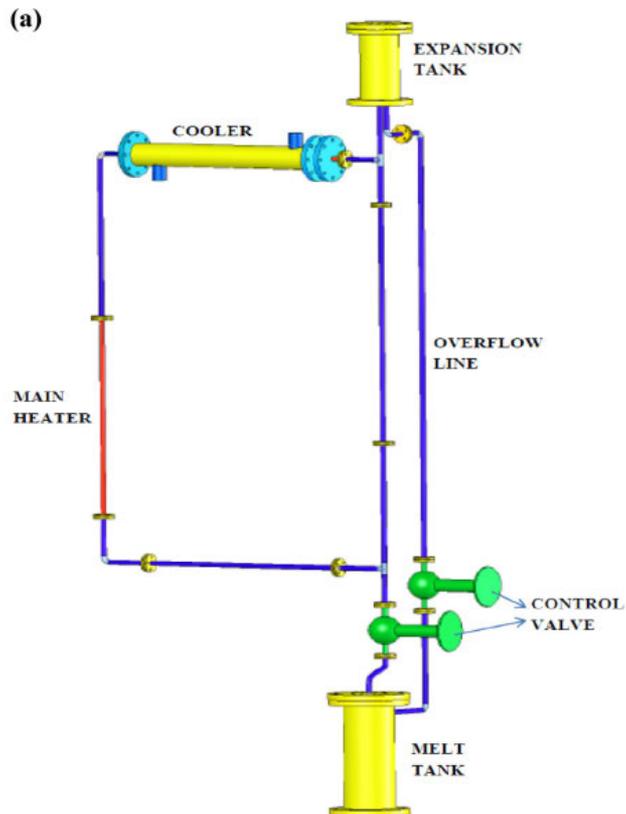
Organization	NC/FC	Experiment Modeling	Objective	Material	Working fluid	Max working temp. (°C)	at max temp. (K ⁻¹)	Max power (kW)	Ref.
Shanghai Institute of Applied Physics, China	NC	Experiment	Gather experience on design and validation of passive decay heat removal system for FHRs	SS 316 Single loop	KNO ₃ -NaNO ₂ -NaNO ₃	450	0.00075	--	[22]
	FC	Experiment	Validate system design; Develop principle prototypes of molten salt pump, valves, HX, etc.	Hastelloy C276 Single loop	FLiNaK	650	0.00032	150	
Beijing University of Technology, China	NC	Experiment	Investigate natural circulation heat transfer of molten salt in a single energy storage tank	SS 316 tank	Ca(NO ₃) ₂ -KNO ₃ -NaNO ₃ -LiNO ₃	250	--	0.3	[23]
Bhabha Atomic Research Centre, India	NC	Experiment In-house developed code LeBENC	Investigate thermal hydraulics, instrument development, and material related issues relevant to high-temperature reactor, such as MSBR	Inconel 625 Single loop	KNO ₃ -NaNO ₃ -LiNO ₃	580	0.0006	2	[24]
	NC	Experiment OpenFOAM	Experiments: a) Steady-state at different power levels; b) Startup transient; c) Loss of heat sink; d) Heater trip; d) Step change in heater power.	Hastelloy N Single loop	LiF-ThF ₄	750	0.00049	1	[25]

Review of Natural/Forced Circulation Loops for MSR/FHR (Cont'd)

Organization	NC/FC	Experiment Modeling	Objective	Material	Working fluid	Max working temp. (°C)	at max temp. (K ⁻¹)	Max power (kW)	Ref.
EU project SAMOFAR	FC	Experiment	Preparation for MSFR FFFFER: Forced Fluoride Flow for Experimental Research	--	FLiNaK	700	0.00032	--	[26] [27]
	FC	Experiment	Study the solidification phenomena of a molten salt						
Czech Republic	FC	Experiment	Experimental program in MSR physics and corrosion flow loop	--	FLiBe	--	--	--	[28]

Bhabha Atomic Research Centre's NC Experiments

- Startup



Startup of natural circulation at 1200 W
(A.K. Srivastava, et al., 2016)

(A.K. Srivastava, et al., 2016)

Heat Transfer Correlations (HTC) in RELAP5

- Define the geometry of heat structure
- For single phase liquid, RELAP5 calculate three heat transfer coefficients
 - find the maximum heat transfer coefficient
 - $h = \max(h_{laminar}, h_{turbulent}, h_{natural})$

User defined geometries	Laminar	Turbulent	Natural
Standard	Nu = 4.36	Dittus-Boelter	Churchill-Chu or McAdams
Horizontal annuli, flow in plate and single tube		Dittus-Boelter	McAdams
Parallel flow in vertical bundle with in-line and staggered rods		Dittus-Boelter-Inayatov	Churchill-Chu or McAdams
Crossflow in vertical bundle with in-line and staggered rods		Dittus-Boelter Inayatov-Shah	Churchill-Chu or McAdams
Parallel flow and crossflow in horizontal bundle with in-line and staggered rods		Dittus-Boelter	Churchill-Chu

HTC for Flow in Circular Tubes in RELAP5 (Cont'd)

- Laminar forced convection (Sallers)
 - $Nu = 4.36$
- Turbulent forced convection (Dittus-Boelter)
 - $Nu = 0.023Re^{0.8}Pr^{0.4}$
- Natural convection (Churchill-Chu)

$$- Nu = \left\{ 0.825 + \frac{0.387Ra^{\frac{1}{6}}}{\left[1 + \left(\frac{0.492}{Pr}\right)^{\frac{9}{16}}\right]^{\frac{8}{27}}}\right\}^2$$

$$- Ra = Gr \cdot Pr \quad Gr = \frac{\rho^2 g \beta (T_w - T_b) L^3}{\mu^2}$$

- Natural convection (McAdams)
 - $Nu = 0.27Ra^{0.25}$

HTC in TRACE

- For single-phase liquid , also take maximum values among laminar and turbulent forced convection and natural convection (NC).
 - $h = \max(h_{laminar}, h_{turbulent}, h_{laminar\ NC}, h_{turbulent\ NC})$
- Geometries
 - Tube
 - Rod bundle
 - Helical Coil
 - Cross Flow

HTC for Flow in Circular Tube in TRACE

- Turbulent forced convection (Gnielinski)

$$- Nu = \frac{(f/2)(Re-1000)Pr}{1+12.7(f/2)^{0.5}(Pr^{2/3}-1)} \quad f = [1.58\ln(Re) - 3.28]^{-2}$$

- Laminar forced convection (Sallers)

$$- Nu = 4.36$$

- Laminar NC

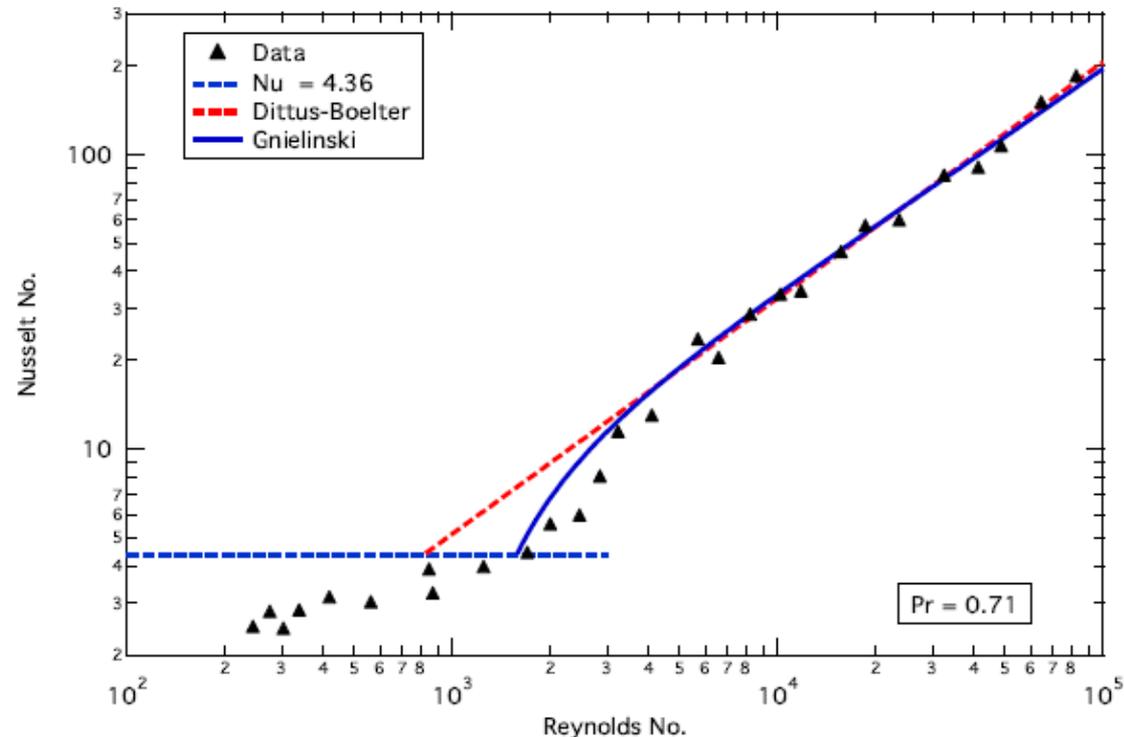
$$- Nu = 0.59Ra^{0.25}$$

$$- Ra = Gr \cdot Pr$$

$$- Gr = \frac{\rho^2 g \beta (T_w - T_b) L^3}{\mu^2}$$

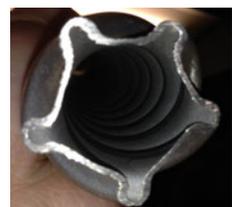
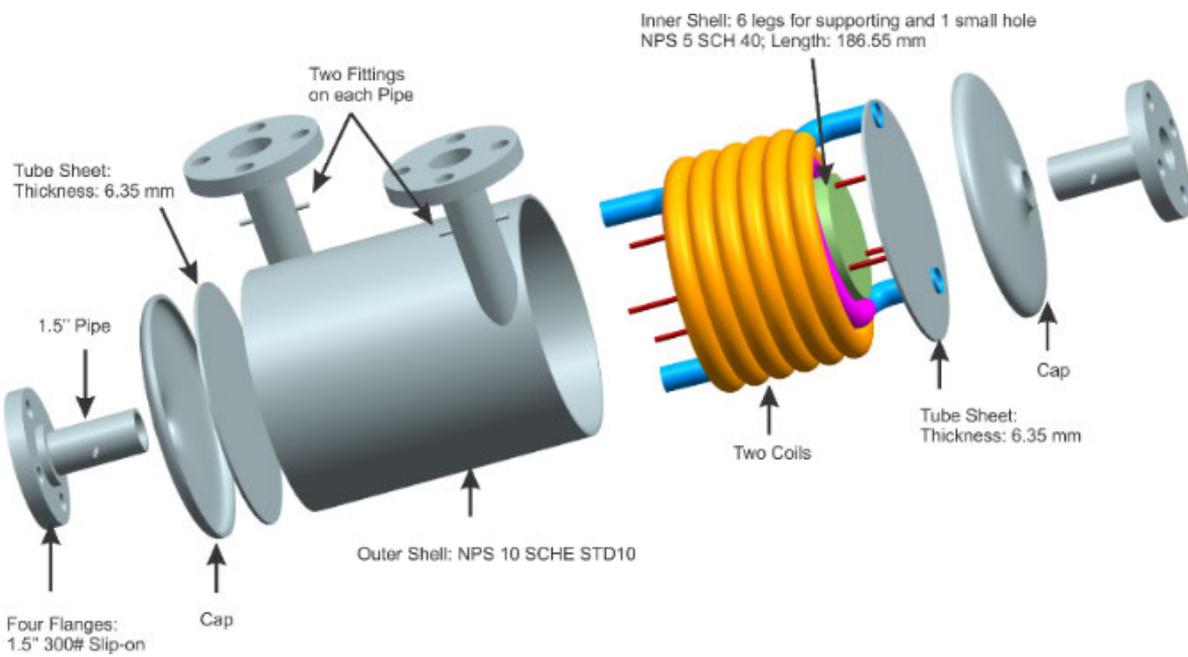
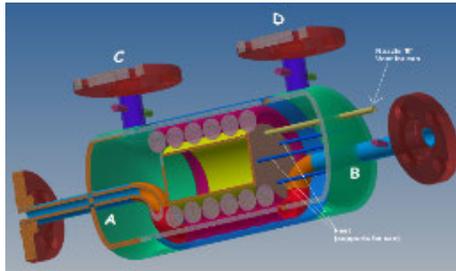
- Turbulent NC

$$- Nu = 0.1Ra^{1/3}$$



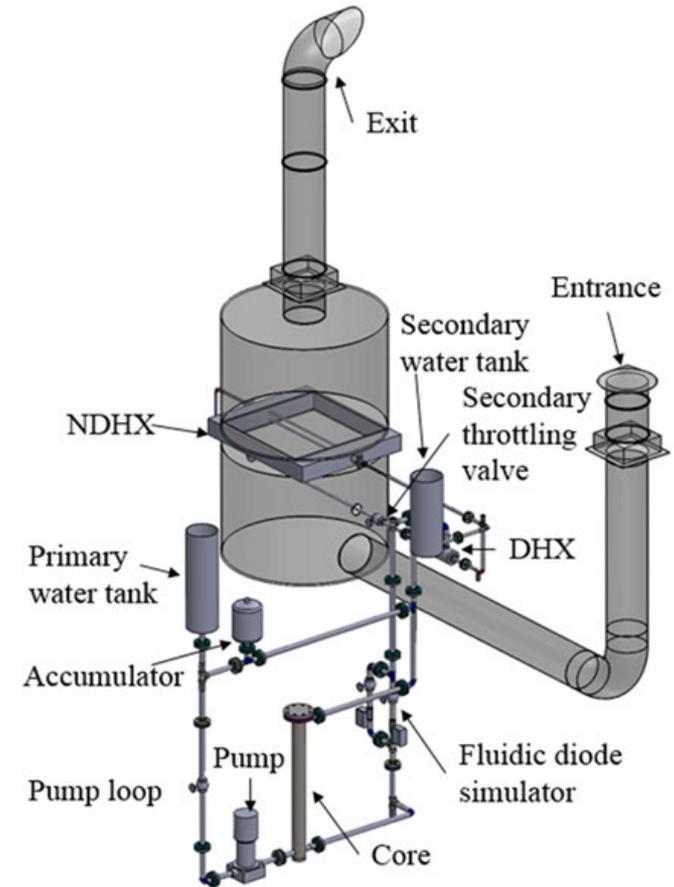
Natural Circulation Heat Transfer in Fluted Tube Heat Exchangers

- HelicALLY-Coiled Fluted Tube Heat Exchangers



Low-temperature DRACS Test Facility (LTDF)

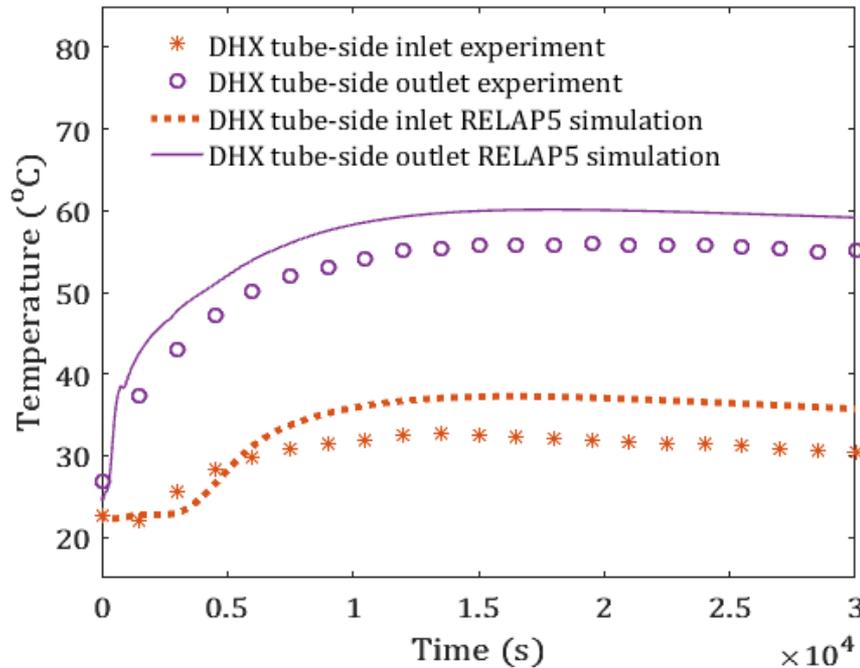
- LTDF Design



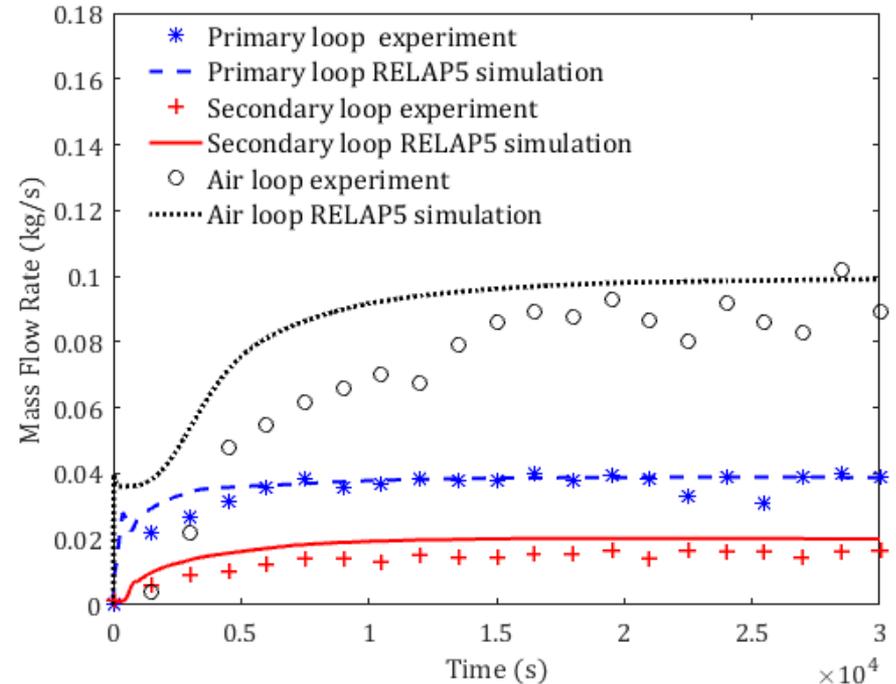
	Primary Water (10 bar)	Secondary Water (1 bar)	Air
T_{hot} (°C)	76.5	65.2	40
T_{cold} (°C)	63.7	34.8	20
ΔT (°C)	12.8	30.4	20
\dot{m} (kg/s)	0.038	0.016	0.102
Loop Height (m)	1.71	0.42	2.1
Pipe ID (cm)	3.7	2.0	35.6

Benchmark RELAP5 Simulation

- DRACS Startup Transient
 - 2 kW from the heater
 - Natural circulation established



DHX tube-side inlet and outlet temperatures

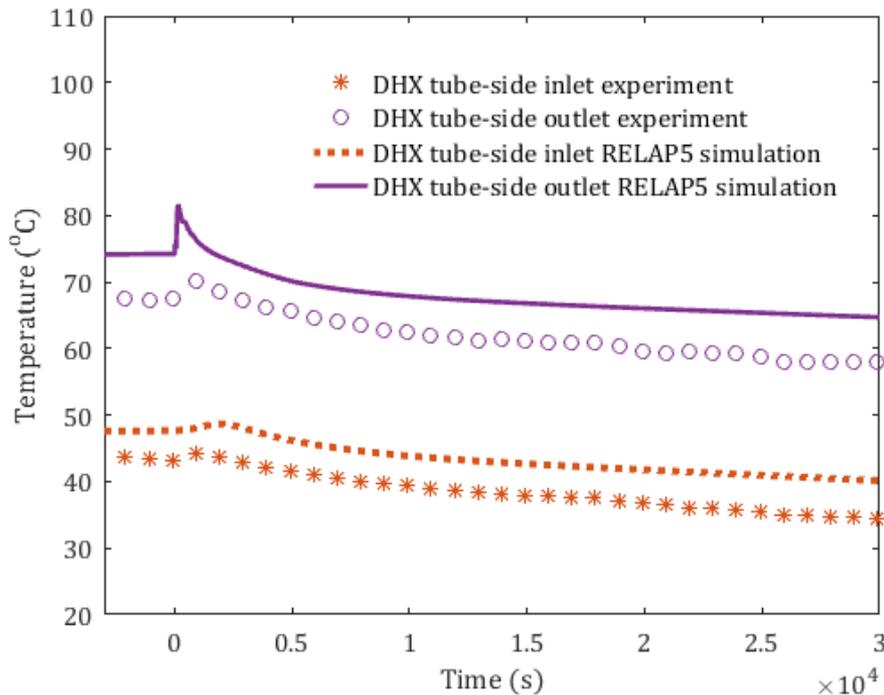


Mass flow rates of three loops

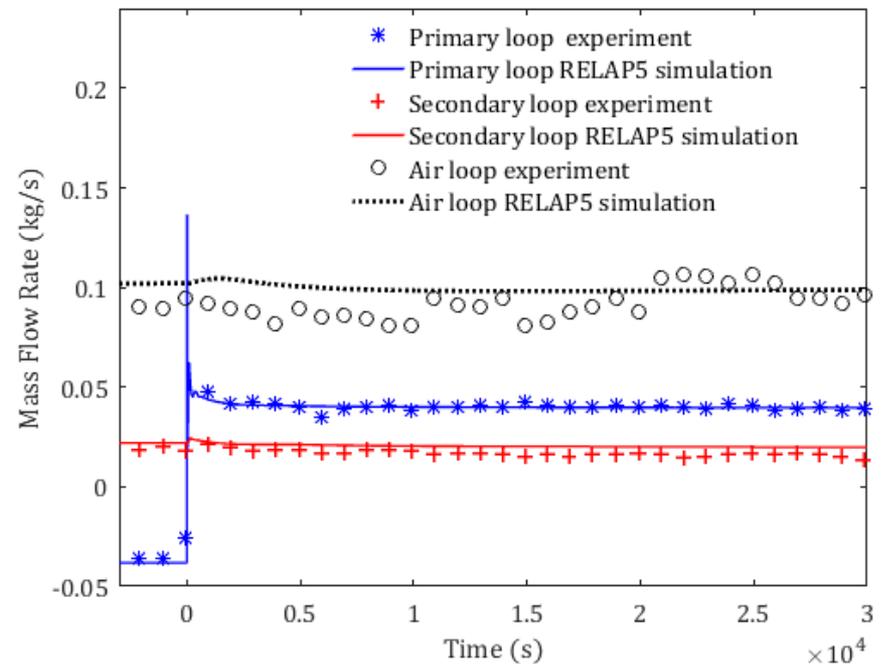
Benchmark RELAP5 Simulation (Cont'd)

- Pump Trip Transient

- Pump tripped when transient initiated
- After pump trip, primary flow reversed and natural circulation flow established

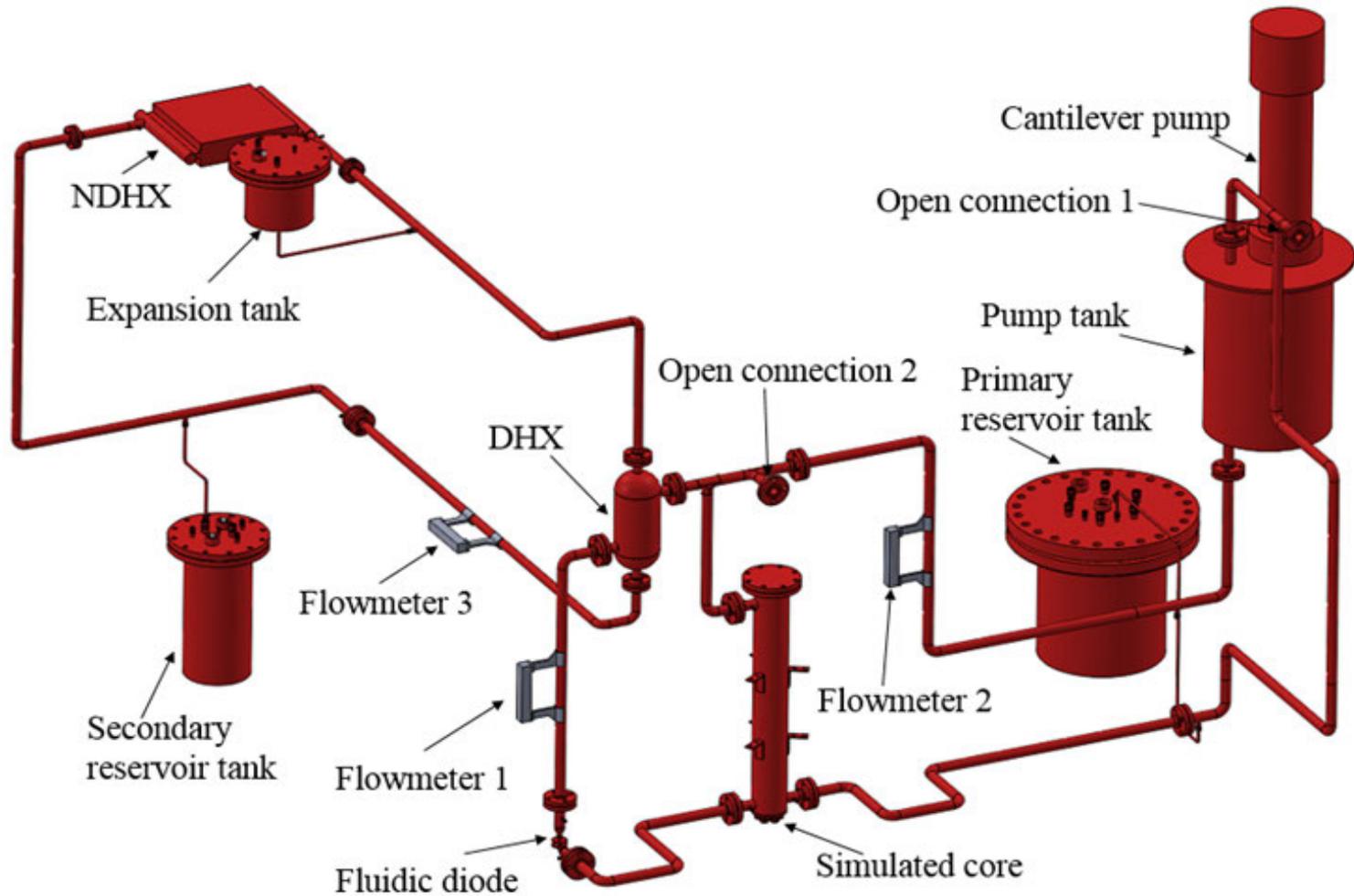


DHX tube-side inlet and outlet temperature



Mass flow rates of three loops

High-temperature DRACS Facility (HTDF)



High-temperature DRACS Facility (Cont'd)



Summary of HTDF Design

- Nominal power: 10 kW

	Primary Fluid (FLiNaK, 0.1 MPa)	Secondary Fluid (KF and ZrF ₄ , 0.1 MPa)	Air
T_{hot} (°C)	722	666	110
T_{cold} (°C)	678	590	40
\dot{m} (kg/s)	0.120	0.127	0.142
Loop Height (m)	1.14	1.08	3.43

- Core: Simulated by 7 cartridge heaters (Max.: 70 kW)
- DHX: Shell-and-tube heat exchanger
 - Shell ID: 211 mm; 80 tubes (5/8") with length: 325 mm; 4 baffles
 - SS 316 as the structure material
- NDHX: Plain-tube heat exchanger
 - 30 tubes (5/8") in 2 rows; tube length: 438 mm
 - SS 316 as the structure material

High-temperature Fluoride Salt Test Facility

- High-temperature Fluoride Salt Test Facility

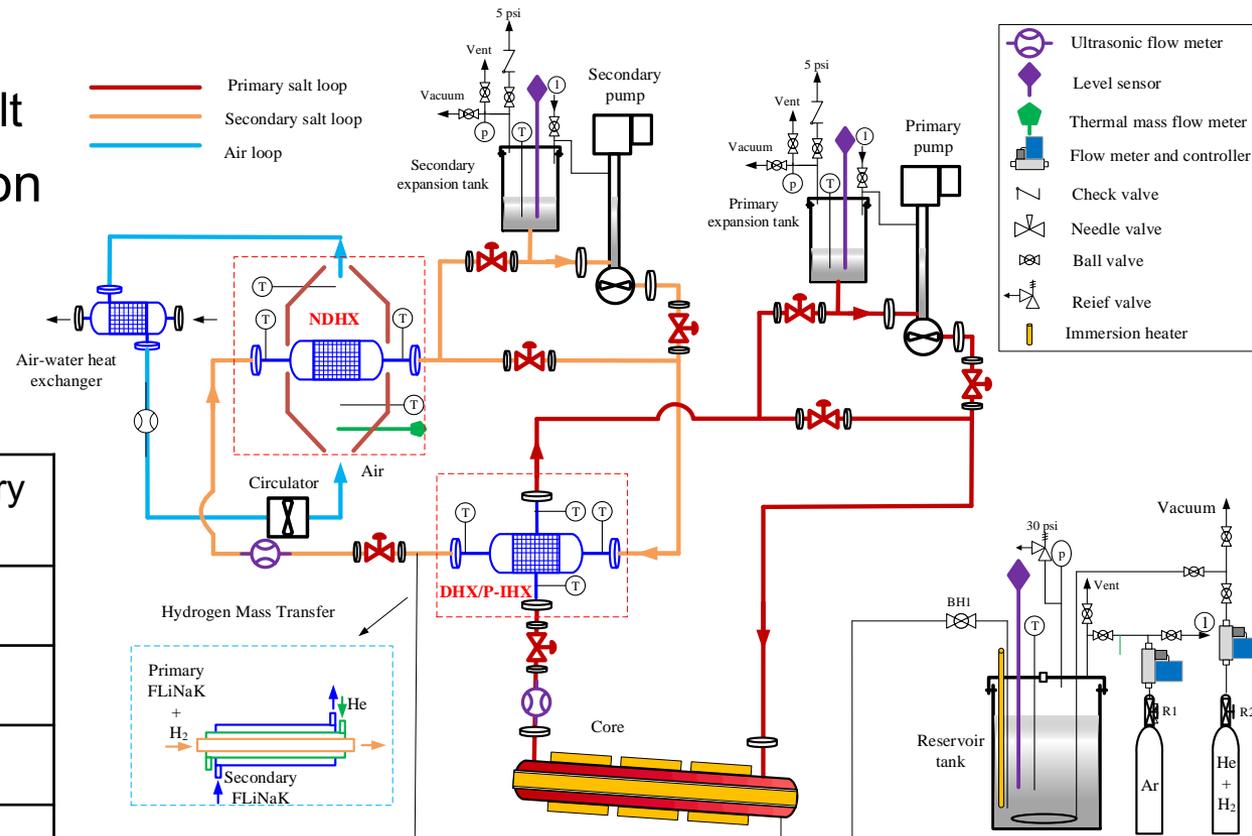
- Natural/Forced circulation

- Primary salt

- Secondary salt

- Forced circulation

- Air



Item	Primary salt	Secondary salt
Salt	FLiNaK	FLiNaK
T_{hot} (°C)	700	587
T_{cold} (°C)	682.7	550
\dot{m} (kg/s)	0.23	0.11
Loop height	1.15	1.22

Summary

- Heat transfer coefficient for salt forced convection:
Existing correlations/models seem to have reasonable accuracy
- Natural circulation salt heat transfer
 - Strongly geometry dependent
 - Thermal radiation effect
 - Experiments for salt natural convection heat transfer
 - Experiments for salt natural circulation

References

- [1] S.W. Churchill and H. Chu, "Correlating Equations for Laminar and Turbulent Free Convection from A Vertical Plate," *International Journal of Heat and Mass Transfer*, **18**, pp. 1323-1329 (1975).
- [2] W.H. McAdams, "Heat Transmission, Third Edition, Chapter 7," McGraw-Hill Book Company, New York.
- [3] R. Fand, E. Morris, and M. Lum, "Natural Convection Heat Transfer from Horizontal Cylinders to Air, Water, and Silicone Oils for Rayleigh Numbers between 3×10^2 to 2×10^7 ," *International Journal of Heat and Mass Transfer*, **20**, pp. 1173-1184 (1977).
- [4] S.W. Churchill, "Free Convection Around Immersed Bodies," *Heat Exchanger Design Handbook*, Section 2.5.7, Begell House, New York (2002).
- [5] F. Incropera, D. Dewitt, "Fundamentals of Heat and Mass Transfer (4th ed)," New York: Wiley (2000).
- [6] <http://www.pathways.cu.edu/ec/Text-PDF/Part%20B-9.pdf>.
- [7] H. Hausen, "Neue Gleichungen für die Wärmeübertragung bei freier oder erzwungener Strömung," *Allg. Warmtech.*, **9**, pp. 75–79 (1959).
- [8] T.L. Bergman and A.S. Lavine, "Fundamentals of Heat and Mass Transfer, Seventh Edition," John Wiley & Sons (2011).
- [9] S. Whitaker, "Forced Convection Heat Transfer Correlations for Flow in Pipes Past Flat Plates, Single Cylinder, Single Sphere, and for Flow in Packed Beds and Tube Bundles," *AIChE Journal*, **18**, pp.361-371 (1972).
- [10] <http://www.pathways.cu.edu/ec/Text-PDF/Part%20B-9.pdf>
- [11] H.C. Savage, E. Compere, J.M. Baker, and E.G. Bahlmann, "Operation of Molten-Salt Convection Loops in the ORR," ORNL-TM-1960, Oak Ridge National Laboratory (1967).
- [12] G. Yoder, D. Heatherly, D. Williams, etc., "Liquid Fluoride Salt Experiment using a Small Natural Circulation Cell," ORNL/TM-2014/56, Oak Ridge National Laboratory (2014).
- [13] D. Felde, E. Ontiveros, D. Fugate, D. Holcomb, K. Robb, and G. Yoder, "Liquid Salt Test Loop Operations," Second Molten Salt Reactor Workshop, October 4-5 (2016).
- [14] H. Lin, "Relap5 Model Benchmark for Thermal Performance of DRACS Test Facilities," Master thesis, The Ohio State University (2016).

References (Cont'd)

- [15] Q. Lv, "Design, Testing and Modeling of the Direct Reactor Auxiliary Cooling System for FHRs," PhD thesis, The Ohio State University (2016).
- [16] N. Zweibaum, R. Scarlat, and P. Perterson, "Verification and Validation of a Single-Phase Natural Circulation Loop Model in Relap5-3D," 2013 Relap5 International Users Group Seminar, September 12-13 (2013).
- [17] N. Zweibaum, J. Bickel, Z. Guo, etc., "UC Berkeley Compact Integral Effects Test (CIET): Facility Design, Test Program, and Initial Validation Studies," Workshop on Molten Salt Reactor Technologies, October 15-16 (2015).
- [19] J. Hughes, A. Wallace, M. Liu, and E. Blandford, "Heat Transfer Research in Support of FHRs at the University of New Mexico, October 16 (2015).
- [18] http://fhr.nuc.berkeley.edu/wp-content/uploads/2016/08/16-002_THWG-White-Paper_FINAL-4.pdf
- [20] P. Sabharwall, M. Ebner, M. Sohal, etc., "Molten Salts for High Temperature Reactors: University of Wisconsin Molten Salt Corrosion and Flow Loop Experiments – Issues Identified and Path Forward," INL/EXT-10-18090 (2010).
- [21] Y. Shin, S. Seo, I. Kim, I. Bang, "Natural Circulation with Dowtherm RP and its MARS Code Implementation for Molten Salt-cooled Reactors," *International Journal of Energy Research*, **40**, pp. 1122-1133 (2016).
- [22] Y. Fu, "SINAP Loop Operations – Summary of Experience to Date," 2016 ORNL MSR Workshop, October (2016).
- [23] L. Wei, Y. Qiang, etc., "Natural Convection Heat Transfer of Molten Salt in A Single Energy Storage Tank," *Science China Technological Sciences*, **59**, pp. 1244-1251 (2016).
- [24] A. Srivastava, J. Kudariyawar, A. Borgohain, S. Jana, N. Maheshwari, and P. Vijayan, "Experimental and Theoretical Studies on the Natural Circulation Behavior of Molten Salt Loop," *Applied Thermal Engineering*, **98**, pp. 513-521 (2016).
- [25] A. Srivastava, R. Chouhan, A. Borgohain, etc., "An Experimental and Numerical Study to Support Development of Molten Salt Breeder Reactor," *Journal of Nuclear Engineering and Radiation Science*, **3**, pp. 031007-1 – 031007-8 (2017).
- [26] <https://indico.math.cnrs.fr/event/601/contribution/9/material/slides/0.pdf>
- [27] M. Tano, P. Rubiolo, and O. Doche, "Progress in Modeling Solidification in Molten Salt Coolants," *Modelling and Simulation in Materials Science and Engineering*, **25**, pp. 1-29 (2016).
- [28] <https://public.ornl.gov/conferences/msr2015/pdf/09-Uhler%20-%20Czech%20exp%20program%20in%20MSR%20physics.pdf>